

1. Approximate  $\sqrt{170}$

$$f(x) = \sqrt{x} \quad f(169) = 13$$

$$f'(x) = \frac{1}{2\sqrt{x}} \quad f'(169) = \frac{1}{26}$$

$$L_a(x) = f'(a)(x-a) + f(a)$$

$$L_{169}(170) = f'(169)(170-169) + f(169) = 13 + \frac{1}{26}$$

2. Approximate  $f(x) = \sin(x + \cos(x))$  at  $x = 170^\circ$ .

$$f'(x) = \cos(x + \cos(x))(1 + (-\sin(x)))$$

$$f'(\pi) = \cos(\pi - 1)$$

$$f(\pi) = \sin(\pi - 1)$$

$$L_\pi(x) = f(\pi) + f'(\pi) \left( \frac{17}{18}\pi - \pi \right)$$

$$= \sin(\pi - 1) + \cos(\pi - 1) \left( -\frac{\pi}{18} \right)$$

3. Let  $f(x) = x\sqrt{4-x}$ , on  $[-2, 4]$ . Find the local and absolute maxima and minima.

$$f'(x) = \sqrt{4-x} + \frac{-x}{2\sqrt{4-x}} = \frac{2(4-x)-x}{2\sqrt{4-x}} = \frac{8-3x}{2\sqrt{4-x}}$$

critical points & endpoints -  $-2, \frac{8}{3}, 4$ .

$$f(-2) = -2\sqrt{6} \quad , \quad f\left(\frac{8}{3}\right) = \frac{8}{3}\sqrt{\frac{4}{3}} \quad , \quad f(4) = 0$$

absolute max:  $x = \frac{8}{3}$       local min:  $x = 4$

absolute min:  $x = -2\sqrt{6}$