## 309 Worksheet 1.1

(1) Are the following statements true or false (circle one):
a) $e$ is a real number and $7<10$. [ true - false ]
b) 119 is a prime number and $\sqrt{3}$ is a rational number. [ true - false ]
c) 119 is not a prime number or $\sqrt{3}$ is a rational number. [ true - false ]
d) $f(x)=e^{x}$ and $g(x)=|x|$ are differentiable at $x=0$. [ true - false ]
e) $f(x)=e^{x}$ or $g(x)=|x|$ are differentiable at $x=0$. [ true - false ]
(2) Are the following statements true or false (circle one):
a) If $a$ and $b$ are integers then $a+b$ is an integer. [ true - false]
b) If $\sum_{i=1}^{\infty}(-1)^{i}\left|a_{i}\right|$ converges, then $\sum_{i=1}^{\infty}\left|a_{i}\right|$ converges. [ true - false ]
c) If $f$ is continuous at $x=0$, then $f$ is differentiable there. [ true - false ]
d) If $\lim _{i \rightarrow \infty} a_{i}=0$, then $\sum_{i=1}^{\infty} a_{i}$ converges. [true - false ]
e) If $x>5$ and $y>5$, then $x y>15$. [ true - false ]
f) If $x>5$ or $y>5$, then $x y>15$. [true - false ]
g) If squares have (only) three sides, then triangles have four sides. [ true - false ]
(3) Rephrase the following statements as 'if - then' statements:
a) The differentiability of $f$ is sufficient for $f$ to be continuous.
b) $k$ is an even integer whenever $k+1$ is odd.
c) For all nonzero real numbers $b$ the square $b^{2}$ is positive.
d) $n m \geq 1$ provided that $n$ and $m$ are nonzero positive integers.
e) For every positive real number $\epsilon$ there is a positive integer $n$ so that $\frac{1}{n}<\epsilon$.
(4) a) Use truthtables to show that the following conditions are equivalent:
( A and B ) and $\mathrm{C}-$ is equivalent to -A and $(\mathrm{B}$ and C$)$
A and $(\mathrm{B}$ or C$)$ - is equivalent to $-(\mathrm{A}$ and B$)$ or $(\mathrm{A}$ and C$)$
b) Show that the following sets are equal:

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(S\capT)\capU=S\cap(T\capU)
S\cap(T\cupU)=(S\capT)\cup(S\capU)
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